MAT 161—Exam #1A—9/16/14

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Calculators are not allowed. Show all work using correct mathematical notation.

1. (24 points) Evaluate each of the following limits, and enter your final answer in the box provided. For this problem, only your final answer will be graded, so there is no partial credit within each part.

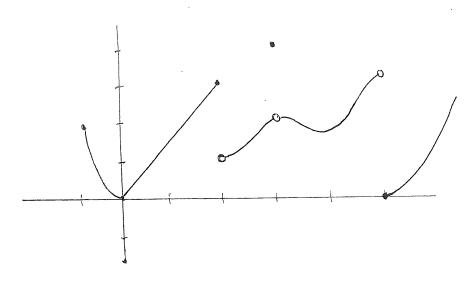
(a)
$$\lim_{x \to 0} \frac{x^2 - 1}{x^2 + 2x - 3} = \boxed{}$$

(b)
$$\lim_{x \to 2} \frac{3x - 6}{x^2 - 4} = \boxed{}$$

(d)
$$\lim_{x \to 0} \frac{\sin x}{x \cos 4x} = \boxed{$$

(f)
$$\lim_{x \to 0} x^8 \sin(1/x^2) =$$

2. (28 points) Consider the function y = f(x) graphed below.



Evaluate each of the following quantities. If a quantity does not exist, say so. Explanations are not required, and there is no partial credit within each part.

(a)
$$\lim_{x \to 2^+} f(x)$$

(b)
$$f(2)$$

(c)
$$\lim_{x\to 3} f(x)$$

(d)
$$\lim_{x \to 5^-} f(x)$$

(e)
$$\lim_{x \to 5} f(x)$$

- (f) The instantaneous rate of change of f at x = 1
- (g) The average rate of change of f on the interval $\left[-1,2\right]$

3. (20 points) Consider the function

$$f(x) = \begin{cases} x^3 - 1 & \text{if } x < 2\\ x^2 + 6 & \text{if } 2 \le x < 5\\ 6x + 1 & \text{if } x \ge 5 \end{cases}.$$

Determine each of the following. If a quantity does not exist, say so. There is no partial credit within each part.

(a) $\lim_{x \to 2^-} f(x)$

(b) $\lim_{x \to 2^+} f(x)$

(c) f(2)

(d) $\lim_{x \to 5} f(x)$

(e) The value(s) of x at which f fails to be continuous

4. (6 points) An object's position along a line is given by the formula $s(t) = t^3$, where s is measured in meters and t is measured in seconds. Find the object's average velocity over the interval $0 \le t \le 2$.

5. (5 points) Suppose that $\lim_{x\to 7} f(x) = 3$. Evaluate $\lim_{x\to 7} \frac{x\cos(\pi x)}{[f(x)]^2}$.

- 6. (5 points) According to the Intermediate Value Theorem, in which of the following intervals is the equation $x^3 - 3x + 1 = 0$ guaranteed to have a solution? There may be more than one answer-circle all that apply!
 - (i) [-2,-1] (ii) [-1,0] (iii) [0,1] (iv) [1,2] (v) [2,3]

7. (12 points) Evaluate $\lim_{x\to 3} \frac{x^2-x-6}{\sqrt{x+1}-2}$, showing all steps using correct limit notation.